

## ELDERLY MORTALITY IN ITALIAN REGIONS AT THE BEGINNING OF THE HEALTH TRANSITION (1881-1921)

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### 1. INTRODUCTION

In this paper we carry out an analysis of the territorial variation of elderly mortality (70–90 years) in Italy during the first stages of the health transition (between the end of the nineteenth and the beginning of the twentieth century).

The period in question includes forty years starting from the census of 1881 till the census of 1921; the territorial detail is that of regions (16 during the period). During this time frame the available data allow us to analyze mortality in four distinct periods, namely in 1881-82, in 1900-01, in 1911-12 and in 1921-22.

It is a well-known fact that, at the beginning of the demographic transition, the main contribution to the increase of life expectancy at birth was given by the decrease of infant, youth and – with a certain delay – adult mortality, while elderly mortality did not vary in a substantial way for a long time on, and in the very first stages of the transition seems actually to have increased. The life tables available at the moment for the overall Italian population<sup>1</sup> show, in fact, a remarkable increase of elderly mortality between 1881 and 1901.

We have therefore tried to check – also by analyzing the regional trends – the hypothesis that at least a share of that increase of the mortality risks could be fictitious, that is, linked to the strong distortion of the age distribution of the population and of the deaths that characterizes the data of 1881. In fact, the distortion could cause an underestimation (Coale and Kisker, 1986; Thatcher, 1992; Preston *et al.*, 1999) of the mortality risks in very advanced age.

We therefore took particular care in the construction of regional life tables based on 1881 census, in order to remedy, as far as possible, the inaccuracy of the data.

The chief aim of the paper was, however, to highlight and to analyze any possible regional pattern of mortality at advanced age in the period of forty years (1881-1921) under consideration.

The paper is structured as follows. The second section deals with the trend of elderly mortality at national level in the forty years analyzed and stresses the un-

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<sup>1</sup> Gini and Galvani (1931), Human Mortality Database (<http://www.mortality.org>)

expected increase of mortality between 1881 and 1901. The third section is devoted to problems linked with the construction of the life tables and of data reliability, especially regarding the 1881-82 tables. The fourth section provides a first look at the overall survival level of people aged 70 and over, in Italy on the whole as well as in the Italian regions, and briefly analyzes the cause mortality structure of the elderly at the beginning of the health transition. The fifth section presents the results of a multiway analysis (Bove and Di Ciaccio, 1994) carried out on the available data according to the STATIS method (Lavit *et al.*, 1994); the aim of the study is to highlight regional differences in elderly mortality during the forty years period under investigation.

## 2. OLD AGE AND VERY OLD AGE AT THE END OF THE NINETEENTH CENTURY

Data in Table 1 show, both for male and female Italian population, the variation – in the forty years under consideration (1881-1921) – in overall survival and in mortality and survival at advanced age, and also allow a comparison with recent years (2006)<sup>2</sup>.

TABLE 1  
*Elderly survival and mortality in Italy, 1881-2006*

	<i>m</i>			<i>f</i>		
	1881-82	1921-22	2006	1881-82	1921-22	2006
$e_0$	35.24	49.24	78.44	35.76	50.72	83.98
$E_0/l_0$	0.2055	0.3638	0.7975	0.2104	0.3931	0.8927
$h_{80}/l_0$	0.0697	0.1308	0.5481	0.0656	0.1424	0.7330
$b_{80}/l_0$	0.0073	0.0089	0.1769	0.0061	0.0118	0.3441
${}_{20}q_{70}$	0.9646	0.9756	0.7781	0.9711	0.9700	0.6145
$e_{70}$	8.20	8.38	14.04	7.80	8.48	17.32
$e_{x=10}$	65.84	67.07	76.18	65.23	67.30	79.72

It is well known that the considerable increase in overall survival between 1881 and 1921 (about 15 years of life in males as well as females) was mainly caused by the sharp reduction of infant and child mortality (Caselli 1990, 1991, 2007; Pozzi 2000; Del Panta 1990). Nevertheless, the survival up to 70 years also had a clear progress during the same period. On the other hand, changes in mortality beyond the age of 70 were very slight. The age at which remaining life expectancy is ten years (which can be considered the threshold of the beginning of old age; see Ryder, 1975) had an increase of barely two years (both for males and females) during the forty years in question, while today (2006) this age has grown (compared with 1881) by more than ten years for males and by nearly fifteen for females<sup>3</sup>.

Still in 1921, people surviving up to 90 years were about one per cent (slightly less for males, a little more for females) of the root of the life table. All in all, the

<sup>2</sup> A description of the long-term trend (1871-2007) elderly survival and mortality in an Italian region (Emilia) is carried out by Rettaroli *et al.* (2009).

<sup>3</sup> This clearly indicates that, also as a subjective perception, the idea of the onset of old age is today very different from that prevailing a century ago.

data of Table 1 justify the decision to concentrate our attention – as far as the period between the end of the nineteenth and the beginning of the twentieth century is concerned – on the analysis of mortality between 70 and 90 years. Moreover, we have decided to neglect (after a first brief analysis at the national level) the gender differences in mortality at advanced age, which remain rather small up to 1921.

In Table 2, age specific mortality rates in three age groups over 60 years are shown, calculated by Tizzano (1965) for several periods between 1870-73 and 1950-53.

TABLE 2  
*Old age specific mortality rates in Italy from 1870-73 to 1950-53*

	Deaths per 1000 inhabitants of the same age groups							
	1870-73	1880-83	1899-902	1909-13	1920-23	1929-33	1934-38	1950-53
Overall population								
60-65	35.0	33.9	32.3	28.3	25.2	24.1	23.3	18.2
65-75	70.3	74.8	65.6	59.8	53.3	49.3	48.4	39.4
above 75	151.0	169.1	180.9	171.4	153.2	144.3	140.8	124.3
Males								
60-65	35.8	34.5	33.6	29.9	26.7	26.6	25.7	22.0
65-75	68.3	72.8	65.5	60.3	54.4	52.4	51.7	43.8
above 75	147.4	164.2	178.4	171.0	153.3	149.6	147.2	131.5
Females								
60-65	34.2	33.2	31.0	26.7	23.7	21.8	21.1	15.2
65-75	72.5	77.0	65.7	59.3	52.2	46.5	45.3	35.8
above 75	154.7	174.2	183.4	171.8	153.1	139.6	135.3	118.5

Source: Tizzano (1965), p.444.

While in the age group 60-65 we can observe a slow gradual reduction of mortality ever since the first ten years period, in the next age group (65-75) a first stage of increase in mortality can be highlighted and the following decrease (starting from 1899-1902) is a little less pronounced. On the contrary, the initial increase of mortality, both for males and females, is very sharp for the age group 75 and over, and continues up to 1899-1902. The subsequent decrease in mortality over 75 years of age leads to mortality levels which in 1920-23 are still slightly higher for males, and scarcely lower for females, compared to those of 1870-73.

The initial increase of mortality levels in the oldest age groups during the first stages of the health transition is therefore a well known phenomenon, even if it is not easy to ascertain to what extent this could be only an apparent trend, that is to say linked to the inaccuracy of the data (the distributions of deaths and population by age) on which the measure of that increase is based (Thatcher, 1992<sup>4</sup>; Preston *et al.*, 1999; Kannisto, 1999). In Section 3 the possible bias of old age mortality measures for the period we have considered will be discussed.

<sup>4</sup> Thatcher (p. 413 and footnote 10) stresses the fact that, particularly as far as ages over 85 or 90 are concerned, if some people's ages are overstated, even if they are overstated consistently both in the census and in the death registrations, the calculated death rates would be too low. He adds that, at ages over 85 or 90 during the early years covered by his study (the first English cohorts considered are those born in 1831-40), the calculated death rates may be too low. As a matter of fact, in Table 4 (p. 417) the expectations of life at ages 85, 90 and 95 (for England and Wales) of the male cohorts born in 1831-40 are higher than those of the cohorts born in 1841-50. Only starting from the cohorts born in 1851-60 an increase in the expectation of life at high ages can be appreciated.

Here, we will initially concentrate on the mortality risks between 80 and 90 years, and consider the long-term trend in some countries, the data for which are drawn from the Human Mortality Database<sup>5</sup> (HMD).

Figure 1 was constructed using the period life tables (both sexes) of three countries (Sweden, France, Italy) in which the beginning of the health transition can be said to have occurred at very different times. At the same time, relevant differences can be noted in the initial date of the continuous registration of deaths allowing the construction of life tables (1751 for Sweden, 1816 for France, 1872 for Italy).

If we observe the figure, we are struck by the fact that in all the three cases we can identify a first stage of increase of the mortality risks between 80 and 90 years. This phase is very precocious in Sweden (from the latest decades of the eighteenth century and up to about 1840). The second country which shows an initial increase in mortality at advanced ages is France, between about 1830 and 1870, but here a subsequent long phase of approximate stability can be observed before the start of the irreversible decline. Finally, starting only in the last decades of the nineteenth century, and lasting a considerably shorter period of time, the same increase can be shown for Italy too.

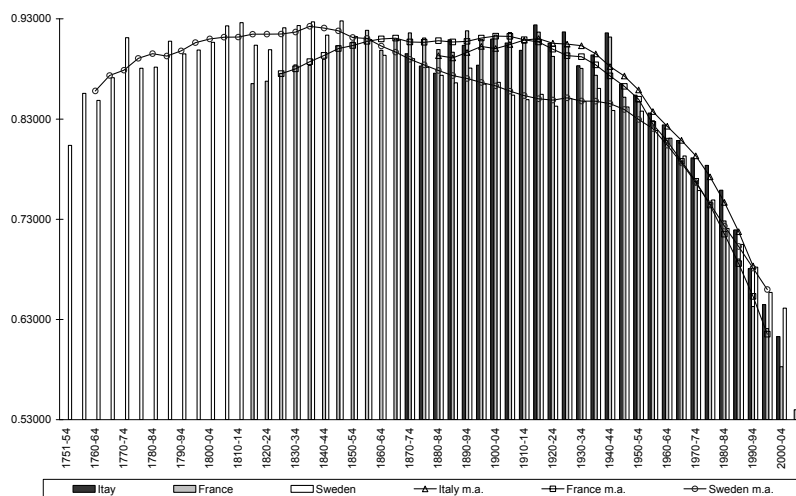


Figure 1 – Probability of dying between 80 and 90 years of age in Sweden (1751-2007), France (1816-2004) and Italy (1872-2004).

As a matter of fact, the aim of this brief analysis concerning three European countries is simply to verify the possibility that in different contexts (both with regard to mortality factors and to the completeness and quality of the data which

<sup>5</sup> The Human Mortality Database provides both abridged and complete life tables. We chose to use abridged life tables referred to every five calendar years, then we smoothed the values with a five-term moving average.

allow the construction of the life tables<sup>6</sup>), an initial increase in advanced age mortality risks may actually be appreciated.

We shall now concentrate on the Italian case and analyse in more detail the trend of the mortality risks between 80 and 90 years of age from 1872 to 1922, illustrated in Figure 2. If we restrict the comparison to 1881-82 and 1900-01 (as we are obliged to if we use only the life tables constructed in census years) we appreciate a strong increase of  ${}_{10}q_{80}$  (this fact bears out data published many years ago by Tizzano (1965) concerning the open class 75+). In fact the values of 1881 and 1882 are among the lowest of the whole period, while the values of 1900 and 1901 are among the highest. If we observe the whole series of the mortality risks, we have the idea of a very high variability. We can in any case also appreciate a moderate, growing trend of  ${}_{10}q_{80}$  between 1872 and 1922.

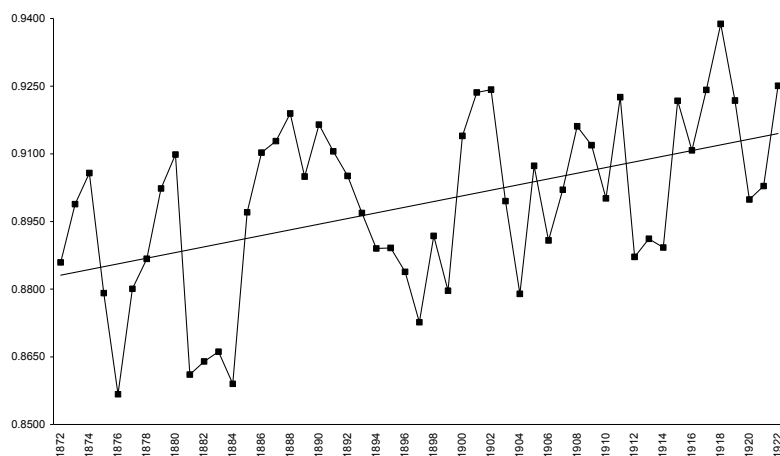


Figure 2 – Probability of dying (both sexes) between 80 and 90 years of age in Italy from 1872 to 1922, according to HMD period life tables.

In general, we cannot exclude the existence of some factors that have actually contributed, in the last decades of nineteenth century and in the first decades of twentieth century, to the reduction of the survival probability of the elderly.

The difficulty in giving a plausible answer in this respect is linked to two different problems. First, we ought to reconstruct, at least approximately, the whole life history (in terms of mortality risks) of the cohorts that were about 80 or 90 years old approximately between 1880 and 1900. Therefore, we are dealing with cohorts that were born at the beginning of the nineteenth century, whose complete cohort life table is impossible to reconstruct. Neither is it possible, for those cohorts, to estimate the percentage of surviving people up to 80 years. For this purpose, the level of  $l_{80}$  that we can draw from the period life tables is not particularly valuable.

<sup>6</sup> The accuracy of ancient Swedish deaths and population registers and, in particular, the quality of age data are well illustrated by Lundström (1995).

On the other hand, we should investigate the main old age mortality causes at the end of the nineteenth century, as trying to explain the possible increases of mortality linked to the worsening of specific conditions. In Section 4 we shall outline the elderly cause specific mortality as far as the period we consider is concerned, but we have to consider, in this case as well, the poor quality of data.

For the sake of argument, we could assume that the very strong selection effected by mortality from the very first instants of life and then through the whole course of life (Caselli *et al.*, 2000; Vaupel and Yashin, 2006) might, in a very distant past, have allowed only very few and highly select people to reach the threshold of old age. Those select individuals could have had a stronger resistance to mortality in the very old ages in comparison to more recent cohorts, when better conditions of life also enabled the achievement of very old ages to less strong individuals.

In fact, several important studies have discussed the possible *debilitation* or *selection* effects of infant and child mortality levels on adult or elderly mortality. As far as the Italian case is concerned, we can cite the pioneer study of Livi Bacci (1962) and the one of Barbi and Caselli (2003). Both of them have faced the problem by analysing the regional differences in elderly mortality. In particular, Barbi and Caselli's results and speculations are very stimulating<sup>7</sup>, but – as they recognize in the discussion of the results (p. 52) – “whether it is the *selection hypothesis* rather than the *debilitation hypothesis* that has a role in differentiating mortality by region and sex is hard to identify, it being quite difficult to distinguish between the effects of selection or debilitation”.

Conversely, Caselli and Capocaccia (1989) deal with the debilitation and selection role of early towards adult mortality at a national level, in a cohort perspective as well. Their analysis considers the Italian cohorts born between 1882 and 1953. As discussing the results of the application of a logistic regression model, they admit that the low mortality above 45 in the oldest cohorts (in comparison with the younger ones) may be caused “by their weakest members being lost through highly selective mortality in childhood and early adult life. By the same argument, the mortality of the younger cohorts could have been raised, because of their more favourable early mortality, which has resulted in a larger number of intrinsically weak survivors” (p. 151). Though the authors look very cautious about this hypothesis, a similar situation could be envisaged as far as the Italian cohorts which had reached an old age between 1881 and 1901 (the ones which were born in the first decades of the nineteenth century) are concerned.

Nevertheless, other hypotheses concerning the factors which may have caused the increase of the elderly mortality in the last decades of the Nineteenth Century could be considered. For instance, the agrarian crisis which significantly reduced the annual per capita calories in Italy for a period of about twenty years starting from the beginning of the Eighties, could have affected, year after year, the weak-

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<sup>7</sup> Taking into account mortality experienced at earlier ages, Barbi and Caselli analyse the geographical differences in mortality among the old and oldest old with reference to Italy and four representative regions (Lombardia, Toscana, Calabria and Sicilia), using longitudinal data obtained by mean of a very complex reconstruction of the mortality history of the cohorts born in 1891 and 1892.

est members of the population, that is to say the elderly. This is one of the possible explanations of the higher level of elderly mortality risks registered in 1901 in comparison with 1881<sup>8</sup>.

### 3. THE CONSTRUCTION OF REGIONAL LIFE TABLES: DATA RELIABILITY

In the period we considered (1881-1921), data published by Dirstat<sup>9</sup> enable the construction of regional life tables around the census years of 1881, 1901, 1911, 1921. With reference to 1921-22 we used the tables constructed by Gini and Galvani (1931). For the three previous periods we had at our disposal unpublished life tables which were constructed in more recent years by researchers<sup>10</sup> of the Department of Statistics of Bologna University<sup>11</sup>.

It is important to note that the measure of mortality risks in old ages is based on very scant amounts of living people and deaths. Moreover, as far as 1881-82 is concerned, the age distribution of the population (and also that of deaths) is quite inaccurate<sup>12</sup>.

In any case, the lack of annual age distributions (concerning sometimes the population age distributions, other times the death age distributions, more often both of them) obliges either to estimate the annual age distributions (Gini and Galvani chose this method) or to estimate five-year probabilities of death starting from five-year specific mortality rates. We chose the second way for the construction of regional abridged life tables, since very similar results can be obtained both by the first or by the second procedure<sup>13</sup>, provided that age recording (concerning population and deaths) is accurate.

The values for advanced age probabilities of death in the 1881-82 life tables must be considered with much more caution. In effect, the five-year age distribution of population in 1881 published by Dirstat shows very important irregularities, especially as far as Southern regions are concerned, doubtless caused by a very inaccurate age statement on the part of the people surveyed. These irregu-

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<sup>8</sup> As a matter of fact, no clear relationship between the annual series of per capita calories and of mortality indicators can be detected for the period including the agrarian crisis (approximately 1880-1900), at least at the national level (Del Pantà and Forini, 1994).

<sup>9</sup> Dirstat is an acronym of "Direzione Generale di Statistica", a section of the Ministry of Agriculture whose task was the production of statistical data.

<sup>10</sup> Under the responsibility of Lorenzo Del Pantà.

<sup>11</sup> Abridged regional life tables were constructed for 1871-72, 1881-82, 1900-01, 1910-12, 1921-22. The methodology (in particular for 1881-82 tables) is stated in Del Pantà (1998).

<sup>12</sup> Generally (apart from a few exceptions) Dirstat publications provide, until 1921, five year age distributions of population and deaths. It is important to note that, in census records, the year of birth was registered only starting from the 1901 census. Previously only age (in years of life) was registered. Therefore, in the 1881 census age statement is still approximate, and age heaping on ages ending in zero also distorts five-year age distributions (Preston *et al.* 1999).

<sup>13</sup> The values of the probabilities of death drawn in our abridged life tables for 1921-22 are very similar, for all the Italian regions, to the values drawn in the complete life tables by Gini and Galvani. The estimate of the five-year probabilities of death has been obtained using the formula proposed by Reed and Merrell (1939).

larities lead to an overestimation of  ${}_5q_{75}$ , not entirely counterbalanced by an underestimation of  ${}_5q_{80}$  (Preston *et al.*, 1999).

After several attempts to correct census five-year age distributions and five-year probabilities of death, we decided to undertake a different way and we constructed from the beginning regional life tables for 1881-82, after having estimated annual distributions of population and deaths. As previously said, with reference to 1881-82 only deaths and population data classified according to five-year age groups (up to the last open interval 100+) are available. Therefore, we split these grouped data into single year of age by applying a cubic spline to the cumulative number of deaths or individuals, in the following form (Mc Neil *et al.*, 1977; Wilmoth *et al.*, 2007):

$$Y_x = \alpha_0 + \alpha_1 x + \alpha_2 x^2 + \alpha_3 x^3 + \sum_{i=1}^n \beta_i (x - k_i)^3 I(x \geq k_i), \quad (1)$$

where  $Y_x$  is the cumulative number of deaths or individuals within year  $t$  up to age  $x$ ;  $\alpha_0, \alpha_1, \alpha_2, \alpha_3, \beta_1, \beta_2, \dots, \beta_n$  are the  $n+4$  parameters that must be estimated;  $I(\cdot)$  is an indicator function and  $k_1, k_2, \dots, k_n$  denote the so-called *knots* (for more details, see Roli, 2008).

Let us now consider (Figure 3) the values of the annual probabilities of death between 50 and 90 years of age (both sexes) of the life table concerning the Italian population (1881-82), which we have constructed using the procedure which has just been explained.

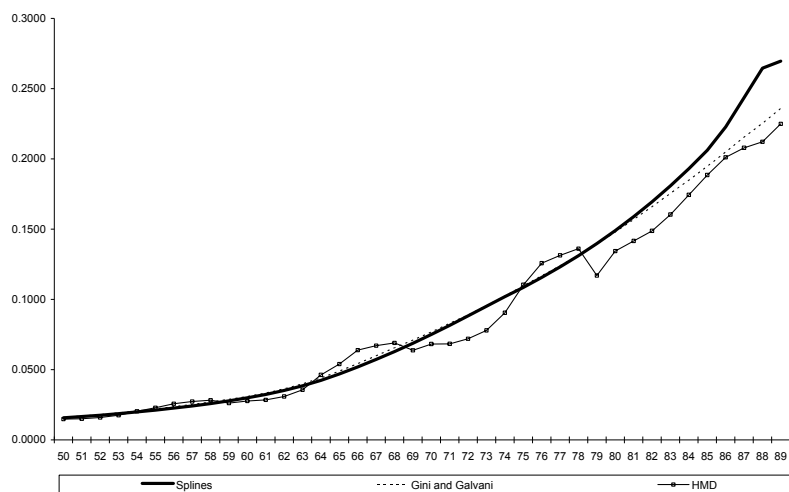


Figure 3 – Italy 1881-82. Annual probabilities of dying from 50 up to 90 years of age obtained by: spline smoothing, Gini and Galvani's tables and HMD tables.

If we compare these values with those drawn from the life table published by Gini and Galvani and with those of the life table (still for 1881-82) of the HMD,



we can easily see that the trend of the  $q_x$  in our life table and the one in Gini and Galvani's table are almost the same up to about 80 years of age, but afterwards our life table suggests slightly higher values. The probabilities of death drawn from the HMD life tables show a rather irregular trend and, in any case, starting from 79 years of age they maintain significantly lower values in comparison both with our life table and with Gini and Galvani's one.

Our belief is that the life tables hitherto at our disposal, which were constructed around the 1881 census (both Gini and Galvani's and HMD's tables, as well as our previous life tables) underestimated mortality beyond 80 years of age, thereby exaggerating the actual increase of elderly mortality which characterizes the end of the nineteenth century.

Moreover, we must stress that, in our opinion, the degree of underestimation of the elderly mortality in 1881-82 varies substantially among Italian regions, and is found to be much stronger in the Southern regions, where the degree of irregularity in the age distribution of the population is substantially higher than the national average. With regard to this, in Table 3 we show the regional values (1881-82) of  ${}_{10}q_{80}$  drawn from our new tables (which will be used in Section 5) compared to the values of the previously constructed abridged tables<sup>14</sup>.

As already mentioned, for all the regions (save for Veneto) the values of the old tables look lower, but the differences between the old and the new tables are minimal in Northern regions and much higher in Southern regions, up to a maximum of 9 per cent in Sardegna.

In fact, the southern Italian regions (especially the ones towards the bottom of the table starting from Puglia) are characterized – as far as the 1881 census is concerned – by an abnormally low ratio between the population totals for the 75-79 and 80-84 age classes. This ratio (for males and females together) is about 1.79 for Italy on the whole, and varies, for southern regions, from 0.88 for Sicilia to 1.10 for Sardegna.

TABLE 3

*Regional values of  ${}_{10}q_{80}$  (both sexes) in 1881-82: comparison between old life tables and new ones (splines)*

	Old (abridged) life tables (1)	New (complete) life tables (2)	(2)/(1)
Piemonte	0.9363	0.9388	1.003
Liguria	0.8502	0.8612	1.013
Lombardia	0.9283	0.9281	1.000
Veneto	0.8982	0.8967	0.998
Emilia	0.8929	0.8934	1.001
Toscana	0.8903	0.8998	1.011
Umbria	0.8524	0.8726	1.024
Marche	0.8925	0.9058	1.015
Lazio	0.9077	0.9162	1.009
Abruzzi	0.8767	0.8897	1.015
Campania	0.8898	0.9095	1.022
Puglia	0.8419	0.8805	1.046
Basilicata	0.8555	0.8950	1.046
Calabria	0.8791	0.9073	1.032
Sicilia	0.8577	0.8976	1.047
Sardegna	0.7780	0.8485	1.091
ITALY	0.8803	0.9015	1.024

<sup>14</sup> See footnote 11.

As far as  ${}_{10}q_{80}$  is concerned, for Italy on the whole the new estimate (0.915) is 2.4 per cent higher both in comparison with our old abridged tables and with Gini and Galvani's tables, but the difference with the value (0.8625) drawn by the HMD tables (see again figure 2) is rather more evident (4.5 per cent).

#### 4. A FIRST LOOK AT THE OVERALL ELDERLY SURVIVAL LEVEL IN ITALY AND IN THE ITALIAN REGIONS

Before undertaking a detailed statistical analysis of the chronological and territorial variations of elderly mortality in the forty years period between 1881 and 1921, we introduce some preliminary data, which provide the general framework of the phenomenon under observation.

Table 4 shows life expectancy at 70 years of age (both sexes) for each of the four dates in question.

It is important to note that, during the course of the forty years in question, the increase of this indicator is very slight (for Italy as a whole from 8.0 to 8.4). It is also interesting to observe that the geographical variability clearly decreases between 1881 and 1921. Finally, we can see that various regions maintain the extreme positions in the regional ranking from the beginning to the end of the period: for instance, Puglia and Liguria are at all times among the regions showing a level well above the national average.

TABLE 4

*Regional life tables (both sexes): life expectancy at 70 years of age and probability of dying between 70 and 85 years (1881-1921)*

	$e_{70}$				${}_{15}q_{70}$			
	1881	1901	1911	1921	1881	1901	1911	1921
Piemonte	7.37	7.61	8.15	8.40	0.9137	0.9154	0.8886	0.8748
Liguria	9.35	8.38	8.76	8.88	0.8124	0.8716	0.8521	0.8436
Lombardia	7.08	7.24	7.68	7.63	0.9132	0.9242	0.9066	0.9026
Veneto	7.98	8.39	8.72	8.86	0.8754	0.8704	0.8594	0.8490
Emilia	7.54	7.61	8.15	8.20	0.8909	0.9073	0.8883	0.8619
Toscana	8.40	7.77	8.26	8.22	0.8525	0.9109	0.8845	0.8829
Umbria	8.50	7.94	8.55	8.26	0.8480	0.8921	0.8720	0.8801
Marche	8.21	7.78	8.31	7.86	0.8740	0.9031	0.8858	0.8987
Lazio	7.42	7.47	7.92	7.85	0.8991	0.9190	0.8950	0.8951
Abruzzi	8.49	8.22	8.74	8.58	0.8528	0.8899	0.8617	0.8706
Campania	8.02	7.90	8.33	8.30	0.8729	0.9002	0.8784	0.8787
Puglia	8.77	7.90	8.88	8.70	0.8388	0.8972	0.8418	0.8564
Basilicata	8.34	7.64	8.48	8.07	0.8471	0.9103	0.8697	0.8890
Calabria	7.87	7.78	9.02	8.44	0.8674	0.9033	0.8331	0.8735
Sicilia	8.85	7.93	8.65	8.72	0.8238	0.8953	0.8598	0.8558
Sardegna	7.66	7.59	8.37	8.66	0.8807	0.9059	0.8733	0.8595
CV	0.0757	0.0401	0.0426	0.0448	0.0341	0.0166	0.0227	0.0204
ITALY	8.00	7.75	8.32	8.43	0.8588	0.9156	0.8729	0.8764

On the contrary, Lombardia and Lazio stand out with very low levels in all the dates. In Section 5 we will go back to some of these regional specificities.

In the same table we report the values of  ${}_{15}q_{70}$  of all the Italian regions. The rationale behind the choice of this indicator as an elderly mortality measure will be illustrated in Section 5.

Let us first consider the values of  ${}_{15}q_{70}$  for the Italian population as a whole: the increase in mortality between 1881 and 1901, which we have already stressed, appears clearly from these data. The later decrease (1901-11) of the mortality risk leads to a level of  ${}_{15}q_{70}$  still a little higher than in 1881, while in 1921 the national level of  ${}_{15}q_{70}$  is close to that of 1911.

If we focus our attention on the first interval (1881-1901), we can see that the mortality increase concerns all the regions (except Veneto) but has very different scopes. As we have already observed, the increase is generally bigger in the regions which in 1881 had lower mortality risks. Indeed, the variability sharply decreases from the first to the second date. Finally, we can note that some regions (Lombardia in particular) maintain along the whole period elderly mortality risks well above the national average, while other regions, like Puglia and Liguria, show consistently lower levels of mortality in advanced age.

It is nevertheless difficult to add more specific remarks to this first brief observation without undertaking a multivariate statistical analysis, which is the object of Section 5. We can, however, make some observations concerning the cause-specific mortality structure which characterized the Italian regions at the beginning of the period in question<sup>15</sup>. As a matter of fact, the distribution of deaths by cause and age groups was published<sup>16</sup> at regional level only for 1888. These data allowed the calculation of cause-specific mortality risks<sup>17</sup> for people aged 60 and over. In Table 5, in the interest of space, we show the values of the rates for large classes of causes and only for four regions which have been chosen as examples. If we consider the values of the rates for Italy as a whole, we can first of all note that mortality caused by infectious diseases was still more than double in comparison with that caused by cancers. At large, in comparison with an overall rate of 74 (per thousand), we can see that the most important groups of causes were the respiratory diseases (nearly 20), and far behind the circulatory and nervous system diseases and senility.

We must stress in particular the high value of the rate attributed to “senility”, as this is a rough and generic definition which precludes any deeper regional analysis, since its value has a very variable level (from 16.2 attributed to Sardegna to 8.6 for Puglia). Despite these difficulties in the analysis, some regional specificities seem noteworthy. For instance, if we compare the cause mortality structure of Lombardia and Sardegna (the latter registers 4.2 points more than the former in senility), we note that Lombardia has higher values for cancers (2.3 points more) and especially for the circulatory system diseases<sup>18</sup> (11.2 points more). For malaria, on the other hand, Sardegna (and at a minor level also Puglia)

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<sup>15</sup> A detailed analysis of the cause-specific mortality structure (without the specification of the age of death) of the Italian regions since the last decades of the nineteenth century and until the end of the First World War was carried out by Mortara (1925). More recently, Pozzi (2000) analysed the evolution of the cause mortality structure in Italy at provincial level. See also Caselli (1990).

<sup>16</sup> Ministero di agricoltura, industria e commercio (1890).

<sup>17</sup> The population above 60 was estimated for 1888 on the basis of the age distributions of population in 1881 and 1901.

<sup>18</sup> We can remember that Caselli and Lipsi (2006) attribute mainly to low levels of circulatory diseases mortality the significant longevity of Sardinians contemporary males.

shows very high values, while this cause of death is nearly absent in Lombardia and in Veneto. Finally, in the latter a noteworthy mortality risk can be attributed to pellagra.

TABLE 5

*Cause specific mortality rates above 60 years (both sexes) per 1000 inhabitants in Italy and in four regions, 1888*

	ITALY	Lombardia	Veneto	Puglia	Sardegna
infectious and parasitic diseases	4.6	3.0	3.4	6.1	8.8
<i>typhoid fever</i>	1.0	0.6	0.8	1.4	0.7
<i>malaria</i>	0.9	0.2	0.2	1.7	2.8
<i>dysentery</i>	0.6	0.1	0.1	0.7	1.4
<i>tuberculosis (all types)</i>	1.2	1.2	1.3	1.3	1.9
neoplasms	2.2	3.1	2.2	1.6	0.8
<i>malignant neoplasms of the stomach</i>	0.6	1.1	0.5	0.3	0.1
rheumatic, nutrition and endocrine glands diseases	1.3	2.2	3.2	0.7	1.0
<i>pellagra</i>	0.7	1.7	2.8	0.0	0.0
nervous system diseases	10.9	13.0	11.1	10.0	8.5
<i>stroke of apoplexy and cerebral congestion</i>	9.1	10.8	9.2	8.5	7.0
diseases of the circulatory system	11.3	15.9	13.6	9.0	4.7
<i>heart diseases</i>	9.6	14.0	10.5	7.5	3.6
diseases of the respiratory system	19.9	17.0	17.5	21.3	20.4
<i>bronchial tubes diseases</i>	6.2	5.2	6.6	6.0	3.9
<i>acute pneumonia</i>	9.9	7.7	8.0	12.0	9.6
diseases of the digestive system	7.2	6.6	5.4	7.0	11.6
<i>enteritis and diarrhoea</i>	4.0	3.4	2.9	4.3	6.2
senility	11.3	12.0	10.2	8.6	16.2
other causes	3.3	3.3	2.9	2.7	3.3
unspecified causes	2.0	1.4	1.5	1.1	3.4
all causes of death	74.0	77.5	71.0	68.0	78.6

Going back to malaria, it is noteworthy to remark that, considering the gender differences in the mortality risks (for all causes) between 80 and 90 years of age in the Italian regions in 1881-82 (Table 6), we can observe very similar values with the exception of the regions where malaria had the highest mortality levels.

TABLE 6

*Probability of death between 80 and 90 years (by sex) in Italian regions, 1881-82*

	<i>m</i>	<i>f</i>
Piemonte	0.9365	0.9415
Liguria	0.8633	0.8596
Lombardia	0.9274	0.9290
Veneto	0.8941	0.8991
Emilia	0.8932	0.8941
Toscana	0.8954	0.9049
Umbria	0.8687	0.8797
Marche	0.9175	0.8954
Lazio	<b>0.8964</b>	<b>0.9317</b>
Abruzzi	0.8804	0.8997
Campania	0.9014	0.9169
Puglia	<b>0.8475</b>	<b>0.9048</b>
Basilicata	0.8957	0.8945
Calabria	<b>0.8895</b>	<b>0.9220</b>
Sicilia	<b>0.8741</b>	<b>0.9163</b>
Sardegna	<b>0.8369</b>	<b>0.8614</b>
ITALY	0.8956	0.9074

In these regions, where in adult ages a prevalence of male mortality can be appreciated in the last decades of the nineteenth century (Del Panta and Rosina,

2002<sup>19</sup>; Angeli and Salvini, 2001), we could perhaps assume a selection effect of malaria which allows only very strong and resistant males to survive up to 80 years of age, and these therefore show a higher resistance in comparison with females between 80 and 90 years of age.

After these introductory remarks, let us turn to a statistical analysis of regional differences in elderly mortality.

#### 5. A MULTI-WAY ANALYSIS OF ELDERLY SURVIVAL INDICATORS IN ITALIAN REGIONS ACROSS 1881-1921: THE STATIS METHOD

The STATIS method (Structuration des Tableaux A Trois Indices de la Statistique) has been introduced by Escoufier (1973, 1980), with the aim of exploring three-way data, handled as a set of  $K$  matrices, by computing Euclidean distances between configurations of points (see, for example, Lavit *et al.*, 1994). As far as the present analysis is concerned, it allows to accomplish the following tasks:

1) *Comparing the  $K$  configurations* (see subsection 5.1):

to compare the configurations of the points (observations) in the  $K$  settings by analyzing their similarity structure, with the aim of investigating a possible relationship among them.

2) *Identification and analysis of the “compromise”* (see subsection 5.2):

to combine the configurations into a common representation of the observations, called “the compromise”. It is analyzed via principal component analysis, whose components can be interpreted through their correlations with the original variables observed in the various settings.

3) *Exploring the common structure* (see subsection 5.3):

to project the units onto the space spanned by the main components (dimensions) of the compromise, in order to analyze communalities and discrepancies.

4) *Exploring across setting discrepancies* (see subsection 5.4):

for each pair of settings, compute the contribution of each unit to the distance between the settings, in order to detect the units that mostly varied their position across the  $K$  configurations.

Some multi-way analysis methods, like the so-called Tucker3 model, are based on flexible models allowing to explore each of the three modes (that is, observations, variables and settings) simultaneously; on the contrary, STATIS analyzes the three-way array as a set of  $K$  slice matrices units $\times$ variables<sup>20</sup>. We used STATIS because it is an exploratory method, thus being the most natural candidate for applications, like the present one, where no true stochastic framework can be formulated.

<sup>19</sup> Del Panta and Rosina attribute to malaria the adult (15-70 years) male higher mortality in the southern Italian regions.

<sup>20</sup> The similarities among these matrices are taken into account in determining the contribution of each matrix to the “compromise”. As an example of a different approach, still applied to multi-way demographic data, see Bellini *et al.* (1992).

The data have been arranged as a three-way array with modes regions×variables×occasions, where:

- variables correspond to 8 demographic indicators: besides  $e_0$ , which attests to the overall survival level of the regions, we selected several indicators as best representing the elderly survival:  $e_{70}$ ,  $e_x=10$ ,  $e_{90}$ ,  $5q_{70}$ ,  $5q_{75}$ ,  $5q_{80}$  e  $5q_{85}$ ;<sup>21</sup>

- occasions are the 4 census years, at the turn of the nineteenth century: 1881, 1901, 1911, 1921.

Italy was considered as a supplementary unit, namely it was ignored when performing the analysis but it was plotted onto the compromise, as well as the 16 regions.

Therefore, the data are stored as 4 separate matrices,  $\mathbf{X}_1, \dots, \mathbf{X}_4$ , each consisting of the measurements of the same 8 variables on the same 16 units taken at a different occasion. For each separate occasion, the data (stored in the generic matrix  $\mathbf{X}_k$ ) have been standardized: in this preprocessing phase, observations were weighted in order to take into account their different population amount (the weights, summing to 1, were computed on the basis of the 1901 census data).

The following phases of the method have been carried out using two distinct options about the weights of the regions, stored in the diagonal matrix  $\mathbf{D}$ : the former was to assign identical weights (that is,  $\mathbf{D}=\mathbf{I}$ , with  $\mathbf{I}$  denoting the identity matrix), the latter was to assign the same weights used in the preprocessing phase. The two options yielded similar solutions, but the former gave rise to neater results which are reported and commented in the following. We note that when uniform weights are assigned to the regions, it means that one is interested in detecting any regional pattern, whatever the size of the region.

The analysis has been carried out using R (<http://cran.r-project.org/>) and SPAD software, version 5.0 (SPAD, 1997; <http://www.cisia.com>).

### 5.1. Comparing the configurations

A pairwise comparison of the configurations corresponding to the 4 occasions is performed by means of the so-called *RV coefficients*:

$$RV_{t,t'} = \frac{\text{trace}(\mathbf{S}_t \mathbf{D} \mathbf{S}_{t'} \mathbf{D})}{\sqrt{\text{trace}(\mathbf{S}_t \mathbf{D})^2 \text{trace}(\mathbf{S}_{t'} \mathbf{D})^2}}, \quad (2)$$

<sup>21</sup> With regard to the elderly survival indicators, we included the age at which remaining life expectancy is ten years ( $e_x=10$ ), which is considered the threshold of the beginning of old age (between 65 and 68 years, both for males and females, in the period under observation), together with the life expectancy at the beginning and at the end of the period of life (70-90 years of age) on which we decided to focus (see section 2). Within that life span, we considered the four distinct five-yearly probabilities of death, by which a more detailed analysis of elderly mortality can be carried out.

We decided to include the general survival level ( $a_0$ ) because its presence turned out not to alter the results (as it could be expected, since it is not an elderly survival indicator) but proved to be relevant in the interpretation of the “compromise”.

where the scalar product matrix  $\mathbf{S}_t = \mathbf{X}_t \mathbf{X}_t^\top$  ( $t, t' = 1, \dots, 4$ ) gives a representation of the mutual relationships (in terms of Euclidean distances) among the regions at occasion  $t$  on the basis of the observed variables, and  $\mathbf{D}$  is a diagonal matrix assigning weights to the regions; from here on,  $\mathbf{D}$  is taken to be equal to the identity matrix.  $RV_{t,t'}$  gives the cosine between the matrices  $\mathbf{S}_t$  e  $\mathbf{S}_{t'}$ , taken in vectorized form; therefore, it takes its maximum value ( $=1$ ) if the compared configurations are identical.

The RV coefficients for the four occasions are reported in Table 7. The results show that a common structure among the four occasions is present, which justifies their simultaneous analysis. In addition, the RV coefficient values are moderately high and decrease with increasing time lag: this suggests that both common and specific features are worth to be analysed.

TABLE 7  
RV coefficients

	1881	1901	1911	1921
1881	1			
1901	0.582	1		
1911	0.524	0.591	1	
1921	0.389	0.567	0.564	1

The similarity structure of the four scalar-product matrices, called interstructure, can be visually analyzed by the eigen-decomposition of the between-occasion cosine matrix  $\mathbf{C} = [RV_{t,t'}]$ : occasions are represented as points in the eigenspace. Concerning the data shown in Table 7, the bivariate representation spanned by the first two principal components is reported in Figure 4. The sum of the corresponding two eigenvalues is about 80% of the overall sum of the eigenvalues.

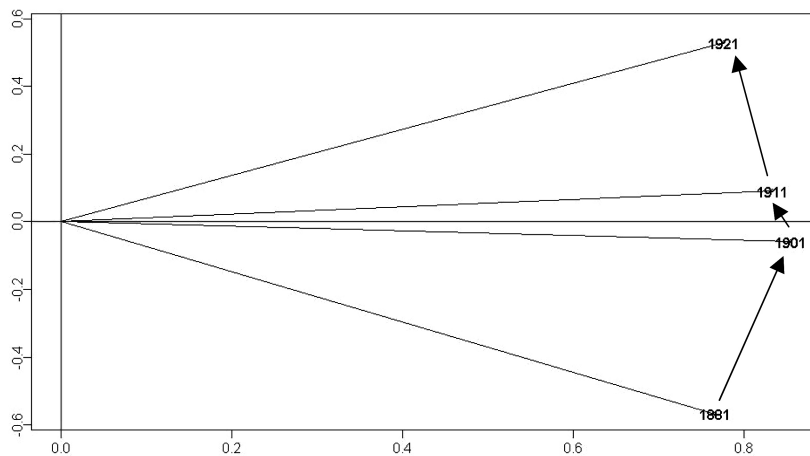


Figure 4 – Similarity structure of the four scalar-product matrices.

The most relevant result visible in the plot is that occasions are nicely ordered in temporal sequence. This means that the structure shared by the occasions changed according to a temporal pattern. It provides an important confirmation to the soundness of the analysis, since the chronological ordering of the four occasions is not contained in the data as “a priori information”.

### 5.2. Identification and analysis of the “compromise”

The so-called “compromise”,  $\mathbf{S}$ , is a weighted average of the scalar-product matrices representing each occasion; the weights are chosen so that configurations agreeing most with other configurations will have the larger weights (for further details, see Lavit *et al.*, 1994). By applying the singular value decomposition  $\mathbf{S}=\mathbf{QLQ}^T$ , with  $\mathbf{Q}^T\mathbf{DQ}=\mathbf{I}$ , the compromise space can be approximated by considering only the most relevant columns of the matrix  $\mathbf{Q}$ .

In the present analysis, the approximation of the compromise provided by the first two principal components explains almost the 70% of the inertia. After restricting attention to the first five components, Table 8 presents the (cumulated) percentage of explained inertia.

TABLE 8  
(Cumulated) percentage of inertia explained by the first five principal components

Dimension	Percentage of inertia	Cumulated percentage of inertia
1	43	43
2	23	67
3	9	76
4	8	84
5	5	89

The two extracted components can be interpreted by analyzing the values of their correlation coefficients with the original variables observed in the various settings (see Table 9). In fact, these correlations are nothing but the coordinates of the original variables onto the compromise.

The first dimension (accounting for 43% of the inertia) can be interpreted as the opposition of indicators  $e_{70}$  and  $e_x=10$  (on the right hand side) to the mortality indicators (on the left hand side). This result sounds reasonable, since:

1) indicator  $e_x=10$  can be likened to  $e_{70}$ , since it takes values around 70 in all the four occasions under investigation. In fact, the correlation between  $e_x=10$  and  $e_{70}$  exceeds 0.93 in all occasions;

2) life expectancy at age 70 globally describes the survival levels after this age; therefore, it is expected to grow with decreasing values of the mortality risks after age 70.

As a consequence, the first dimension can be interpreted as an overall indicator of old people survival/mortality.

The second dimension (accounting for 23% of the inertia) represents a contrast between  $e_0$  (on the right hand side) and  $e_{90}$  (on the left hand side), with the only exception of variable  $e_{90}$  in occasion 1921 which shows a slight correlation with the component.



TABLE 9  
Correlations of the original variables with the first two dimensions of the compromise

	1881		1901	
	Dim. 1	Dim. 2	Dim. 1	Dim. 2
$e_0$	0.227	0.590	0.044	0.925
$e_{70}$	0.837	0.034	0.874	0.405
$e_{90}$	0.237	-0.771	0.206	-0.826
$e_s=10$	0.721	0.202	0.846	0.424
$sqr_{70}$	-0.702	-0.296	-0.735	-0.599
$sqr_{75}$	-0.825	0.049	-0.914	-0.232
$sqr_{80}$	-0.778	0.386	-0.797	-0.160
$sqr_{85}$	-0.440	0.130	-0.383	0.736
	1911		1921	
	Dim. 1	Dim. 2	Dim. 1	Dim. 2
$e_0$	-0.053	0.778	-0.014	0.902
$e_{70}$	0.913	-0.070	0.880	0.049
$e_{90}$	0.266	-0.768	0.258	-0.229
$e_s=10$	0.899	-0.016	0.892	0.075
$sqr_{70}$	-0.904	-0.013	-0.862	-0.092
$sqr_{75}$	-0.803	-0.161	-0.823	-0.083
$sqr_{80}$	-0.791	0.410	-0.803	0.083
$sqr_{85}$	-0.600	0.353	-0.556	0.278

This opposition is confirmed by the negative values of the correlation coefficient between  $e_0$  and  $e_{90}$  in the four studied occasions (the correlation coefficient is equal to -0.236 in 1881, -0.668 in 1901, -0.535 in 1911 and -0.142 in 1921). At first sight, the opposition of these indicators along the second component seems unexpected, since they both are survival indicators. More specifically, life expectancy at birth summarizes the overall survival level across all age groups (in the period under investigation, due to high infant mortality rates, it is highly sensitive to the rate of death in the first few years of life), whereas  $e_{90}$  reflects the mortality level of very old people.

A tentative explanation could be given by conjecturing once again a kind of *selection* effect, as discussed in Section 2: it could be argued that, under low overall survival levels, only a few selected individuals can reach old age, thus producing relatively high values of old age survival probabilities. This interpretation needs some caution since it must be stressed that the observed demographic indicators are computed on the basis of cross-sectional mortality tables; they do not come from the longitudinal study of a generation until the end, hence they show a picture resulting from very heterogeneous patterns and experiences.

### 5.3. Exploring the common structure

The coordinates of the regions onto the compromise are computed through the matrix  $\mathbf{F}=\mathbf{QL}^{1/2}$  and represent the position of the regions in the common structure shared by the different occasions. They are shown in Figure 5.

It is worth noting that Italy (Regno), which has been projected as well as a supplementary unit, is placed near the origin of the axes, as it could be expected since Italy summarizes the different demographic patterns of the 16 regions.

The positions of the regions can be interpreted on the basis of the interpretation of the axes given in Section 5.2. Lombardia and Lazio are placed as extreme

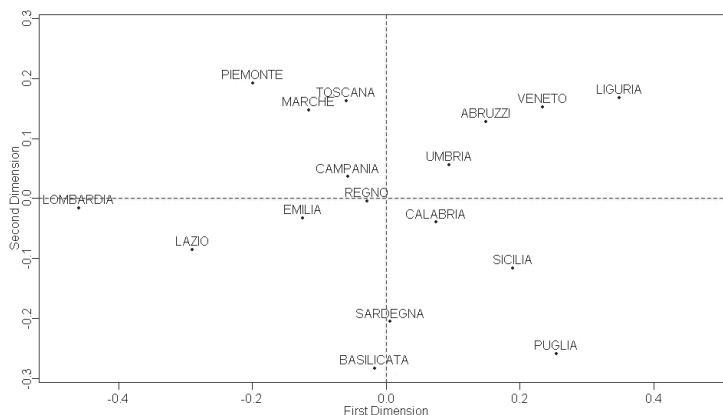


Figure 5 – Projections of the regions on the bivariate approximation of the compromise.

points in the negative half-plane of the first dimension: this means that, in the 40 year period we considered, they are characterized by the lowest old age survival levels. On the opposite side, Liguria, Veneto and Puglia come out among the most favourite regions in terms of longevity. These patterns are visible also by comparing the regions with respect to the values of  $e_{70}$  and  ${}_{15}q_{70}$ , reported in Table 4, that can be deemed to represent the first dimension in its positive and negative senses, respectively<sup>22</sup> (as illustrated in Section 5.2). In fact, Liguria and Puglia stand out as the regions where life expectancy at age 70 mostly exceeds the national value, taking the 40 year period under investigation as a whole; on the other hand, by considering their average behaviour as before, these regions are best ranked in terms of  ${}_{15}q_{70}$ . On the contrary, Lombardia and Lazio are, on average, the most disadvantaged regions with respect to old people survival.

If we focus attention on the interpretation of the second dimension, it can be seen that Basilicata, Puglia and Sardegna are placed in the lowest part of the plot, well separated from the remaining regions. This suggests that, in the common space given by the compromise, these regions have the best performance in terms of very old people life expectancy, while being mostly disadvantaged as far as overall survival levels are concerned. In the latter respect, this result is coherent with the well known fact that Southern and Insular Italian regions (with the partial exception of Sardegna) have been characterized for a long time by higher levels of infant and child mortality with respect to Central and North regions.

#### 5.4. Exploring across-setting discrepancies

A simple and immediate way to describe the across-setting discrepancies and to highlight which units they are mostly due to, is to project each scalar-product

<sup>22</sup> It is worth mentioning that the latter indicator was preferred to  ${}_{20}q_{70}$  because the probability of death between ages 85 and 90 years are only slightly related to the considered dimension (see Table 9).

matrix  $\mathbf{S}_t$  onto the compromise. In the resulting plot the dynamic followed by each region across occasions can be graphically described as a trajectory and can be interpreted w.r.t. the dimensions defining the common space. However, this approach yields good results only if the compromise is a good representative of all the configurations corresponding to the different occasions, that is, if all the RV coefficients are near to 1 (see Bolasco, 1999).

A different approach, which is valid under any condition, is to decompose the discrepancy between occasions  $t$  and  $t'$  ( $t \neq t'$ ) into the contributions given by the different units. More precisely, the contributions given by the different units to the squared distance between the configurations  $\mathbf{S}_t$  and  $\mathbf{S}_{t'}$  are contained in 16-dimensional vector  $\mathbf{dist}_{t,t'}$ :

$$\mathbf{dist}_{t,t'} = \frac{\text{diag}[(\bar{\mathbf{S}}_t - \bar{\mathbf{S}}_{t'}) \mathbf{D}]^2}{\text{trace}[(\bar{\mathbf{S}}_t - \bar{\mathbf{S}}_{t'}) \mathbf{D}]^2}, \quad (3)$$

where

$$\bar{\mathbf{S}}_t = \frac{\mathbf{S}_t}{\sqrt{\text{trace}(\mathbf{S}_t \mathbf{D})^2}}. \quad (4)$$

Unlike the “graphical approach”, based on trajectory plotting, this solution yields exact results, since the decomposition in (3) is based on algebraic calculus.

In the present application, this decomposition yields a set of  $4 \times (4-1)/2$  vectors that allows to detect which units are perturbed when passing from one occasion to another. Due to the temporal sequence of occasions, only pairs of contiguous occasions have to be considered. Results are reported in Table 10. In the following, only the most relevant contributions will be highlighted and commented. For better readability, the features emerged through these analyses will be also shown in terms of trajectories, being aware that trajectories represent an approximation of such patterns.

TABLE 10  
*Percent contributions of the regions to the discrepancies between contiguous occasions*

	1881-1901	1901-1911	1911-1921
Piemonte	5.61	3.90	7.14
Liguria	8.24	7.03	5.54
Lombardia	9.76	12.14	13.79
Veneto	<b>18.35</b>	8.65	7.29
Emilia	3.05	2.66	1.21
Toscana	3.73	1.60	0.87
Umbria	3.30	2.92	2.74
Marche	3.13	2.60	6.31
Lazio	5.43	5.56	4.47
Abruzzi	6.49	4.59	1.42
Campania	1.86	2.60	2.22
Puglia	4.93	11.04	12.34
Basilicata	6.23	8.51	7.10
Calabria	1.10	<b>19.76</b>	<b>18.74</b>
Sicilia	6.60	1.59	4.46
Sardegna	12.20	4.86	4.36

An important caveat that must be taken into account when interpreting the changes of a given region across the years is that these changes are referred to the overall dynamic of the phenomenon, because the method works on centered data matrices (which have been referred to as  $\mathbf{X}_1, \dots, \mathbf{X}_4$  in Section 5.1). This implies that, for example, a high contribution of a unit could be due to the fact that this unit remains quite stable despite the whole phenomenon is highly dynamic.

For the purpose of commenting the relevant contributions as deviation from the overall dynamic of elderly mortality, in the following we will resort to the data in Table 4, which provide synthetic information about the first (and main) dimension of the compromise.

In light of the results in Table 10, the regions showing the most relevant contributions are Veneto, as far as the comparison between occasion 1881 and occasion 1901, and Calabria, for both the remaining comparisons. It is worth noting that each of these three contributions is above the threshold  $Q_3 + 1,5(Q_3 - Q_1)$ , where  $Q_1$  and  $Q_3$  respectively denote the first and third quartile of the elements in the corresponding vector  $\mathbf{dist}_{i,j}$ . This confirms the relevance of the above mentioned contributions.

In effect, Veneto represents an exception to the overall dynamic followed by Italian old people mortality between 1881 and 1901. As it has been already described in Section 2, in that period of time the probability of dying between ages 70 and 90 years underwent a considerable increase. Conversely, Veneto is the only region where  ${}_{15}q_{70}$  does not increase; moreover, among the few regions showing some increase in life expectancy at age 70, it stands out with the highest gain (see Table 4). This is confirmed by inspecting the trajectories of the regions across 1881 and 1901, which can be drawn by comparing the two upper panels of Figure 6. In 1881, Veneto is placed near the origin along the first dimension, which means that it shares the national levels of old age survival. In 1901, it moves to the outermost position in the positive half-plane, thus revealing its relative advantage with respect to the overall pattern.

Since the early twentieth century old age survival starts going up again, although only slightly: in particular, life expectancy at age 70 follows a slight positive trend (see Table 4) while  $e_{90}$  remains quite stable. These considerations should be taken into account when interpreting the results dealing with the comparison between 1901 and 1911 and the one between 1911 and 1921. Throughout both these periods, Calabria is the region that mostly contributes to the distances between contiguous occasions.

Concerning the changes between 1901 and 1911, Calabria is characterized by the highest increase in the values of  $e_{70}$ , while moving from average levels to the lowest ones with respect to  ${}_{15}q_{70}$  (see Table 4). This is confirmed by inspecting the trajectories of the regions across 1901 and 1911, obtainable by comparing the upper right and the lower left panels of Figure 6. In 1901, Calabria is placed near the origin along the first dimension, whereas in 1911 it takes the rightmost position in the positive half-space. Turning back to Table 4, we can see that the remaining southern regions share a similar trend along the first axis, which however is less

pronounced than the one of Calabria; Campania represents an exception, since, like in the northern regions, its improvement in old age survival is less than the one registered in the whole nation.

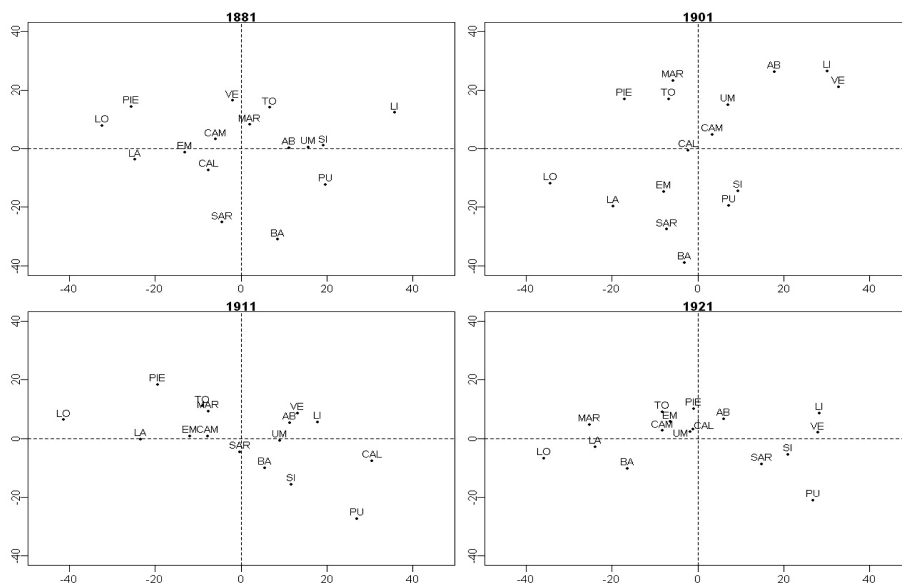


Figure 6 – Projections of the regions on the compromise in each occasion: Piemonte (PI), Liguria (LI), Lombardia (LO), Veneto (VE), Emilia (EM), Toscana (TO), Umbria (UM), Marche (MAR), Lazio (LA), Abruzzi (AB), Campania (CAM), Puglia (PU), Basilicata (BA), Calabria (CAL), Sicilia (SI) and Sardegna (SAR).

In the ten-years between 1911 and 1921, Calabria shows the most relevant contribution, once again, although in the opposite direction (see the two lower panels in Figure 6). In particular, as shown by the data reported in Table 4, it shows the greatest decrease in old age survival indicators: more precisely, the highest increment in the values of  ${}_{15}q_{70}$  is registered, while the levels of  $e_{70}$  show the highest decrease. However, the modifications observed in Italian regions during this time interval are only very slight, in absolute terms, and the patterns of old age mortality can be deemed to be quite stable.

Finally, it is worth noting that the above-mentioned trajectories involve mainly the first dimension of the compromise. This is not surprising, since the second one accounts for only the 23% of inertia. In addition, it can be observed that the second dimension becomes less and less important throughout the occasions: by comparing the panels in Figure 6, a sort of “flattening trend” is visible, *i.e.* the points tend to become more scattered along the first axis than along the second one. As a consequence, the differences with respect to the second axis become less relevant in the interpretation of the results.

Before concluding, it can be interesting to compare the trajectories drawn by Lombardia and Veneto, plotted in Figure 7.

It can be pointed out that the corresponding convex hulls do not intersect, with Lombardia on the left and Veneto on the right. This confirms that in these regions the levels of elderly mortality are different from each other, and that the discrepancy gets larger during the period under investigation. More specifically, in 1881 Lombardia is ranked in the lowest positions as far as elderly survival levels are concerned, while Veneto is in line with national values; after 40 years, Lombardia remains quite stable around the relatively low initial values, while Veneto augments its advantage.

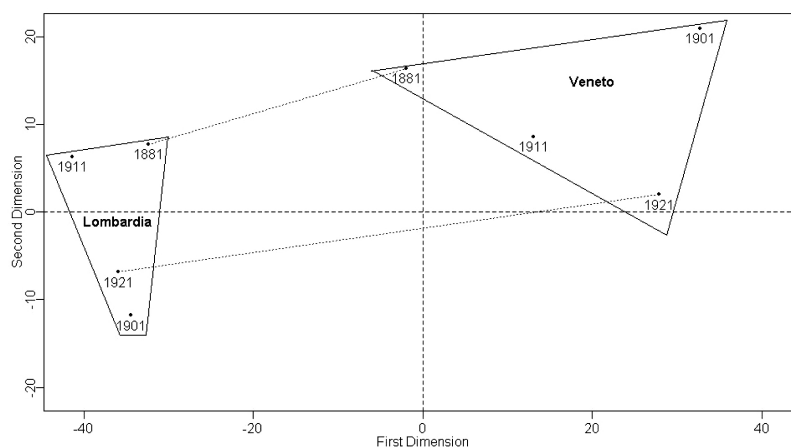


Figure 7 – Trajectories drawn by Lombardia and Veneto.

## 6. CONCLUDING REMARKS

While many authors have analyzed in detail, with reference to Italy, the chronological trend and the territorial differences of child and adult mortality at the beginning of the health transition, little attention has been paid up to now to the characteristics of elderly mortality.

In this paper, we focused our attention on the increase of elderly mortality at the beginning of the health transition (1881-1901) and on the possibility that it is partly due to the inaccuracy of the data. New complete regional life tables for 1881 were constructed by splitting five-year distributions of population and deaths using spline interpolation. On the new tables the increase of elderly mortality between 1881 and 1901 was still evident but had a minor size, especially for Southern regions, whose census and death age distributions are less accurate. Such a feature and the results of the multiway analysis carried out on the data were tentatively explained by resorting to the so-called *selection* hypothesis (that is, some individuals are frailer than others, and the frailer die first). This hypothesis was found to be a possible partial explanation of both territorial and chronological differences in elderly mortality.

A far as the territorial differences are concerned, our study highlighted the permanence for some regions of relatively high/low levels of elderly mortality (namely, Liguria and Puglia on one side and Lombardia and Lazio on the other one). Moreover, Veneto resulted to be atypical with regard to both data quality and the elderly mortality trend between 1881 and 1901.

These results could be the starting point for further investigations at a regional level aiming at revealing the causes of such differences. For example, an insight in cause-specific mortality of Sardegna pointed out that this region stands out in 1888 for extremely low values of mortality for circulatory system diseases. This fact can be related to the relatively low elderly mortality of contemporary Sardinian males observed by Caselli and Lipsi (2006).

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#### SUMMARY

*Elderly mortality in Italian regions at the beginning of the health transition (1881-1921)*

The paper aims to highlight and analyze possible regional patterns of mortality at advanced age (70-90 years) in Italy at the turn of the nineteenth century. The available data are referred to four distinct occasions, namely 1881-82, 1900-01, 1911-12 and 1921-22. After focusing attention on several elderly mortality indicators, we propose to analyze the resulting three-way array (with modes regions×indicators×occasions) using the STATIS method. As a critical preliminary step, new regional life tables for 1881-82 are constructed in order to reduce the possible bias due to the inaccuracy of the age distribution of the population and of the deaths in 1881. The resulting life tables are compared with Gini and Galvani's ones and those available in the Human Mortality Database.